

A Survey on the Privacy-Preserving Applications of Secure Transformation in Collaborative Supply Chains

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1. INTRODUCTION

- Supply chain – complex network composed of suppliers, manufacturers, retailers, and customers
- Collaborative supply chain – two or more participants collaborate
- Solving the problem requires knowing all the information
- Collaborators have private data
- Privacy-preserving techniques: secure multiparty computation (MPC) and secure transformation (ST)

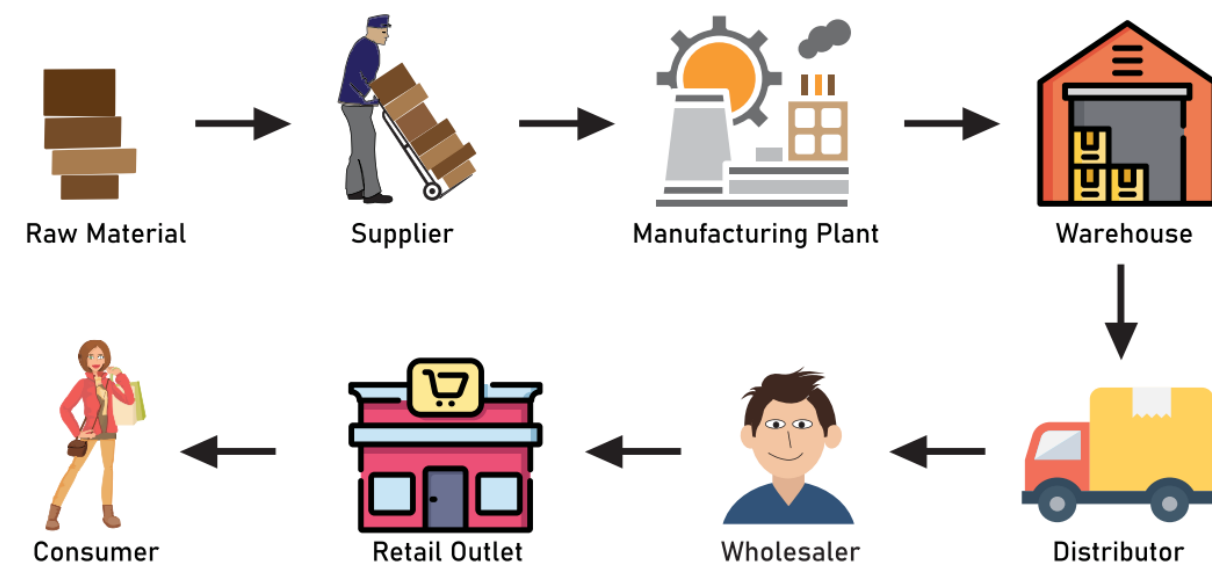


Figure 1: Traditional supply chain [1]

OBJECTIVES

- **Main research question: "How do secure transformation applications preserve privacy in collaborative supply chains?"**
- Find out how MPC and ST work
- Find advantages and disadvantages of each approach
- Discuss feasibility for real-life applications

2. METHOD

- Literature review of privacy-preserving collaborative techniques
- Present the general form of a transformation
- Explain how ST solves problems
- Consider if it is good enough for real-life applications

3. RESULTS

PROBLEM STATEMENT

- The optimal solution is the output of a **function** with multiple inputs
- Collaborators try to find the solution, **without** revealing private information
- Besides the function: **variables**, and **constraints**

A GENERIC TRANSFORMATION

$$\begin{aligned} \min c^T \mathbf{x} & \quad \longrightarrow \quad \min c^T Q Q^{-1} \mathbf{x} \\ \text{s.t. } M \mathbf{x} \geq B & \quad \longrightarrow \quad \text{s.t. } M Q Q^{-1} \mathbf{x} \geq B \\ \mathbf{x} \geq 0 & \quad \longrightarrow \quad Q^{-1} \mathbf{x} \geq 0 \end{aligned} \quad [2]$$

- $MQ = M'$, $Q^{-1}x = y$, and $c^T Q = c'^T$, with Q an invertible matrix
- x is a vector of **variables**
- c is a vector of **objective function coefficients**
- M is a matrix of **constraint coefficients**
- B is a vector of **constraint values**

SECURE TRANSFORMATION

- Relies on transforming the input and the problem
- Result to the original problem found by inverting the transformation [3]
- Usually solves linear programming problems
- Advantage: tailor made transformation to solve a certain problem, fast
- Disadvantage: only heuristic security in most cases [2], non-cryptographic
- Recent developments: revised older transformations; pointed out issues; proved impossibility outside of finite fields [4]; showed usefulness in outsourcing to the cloud

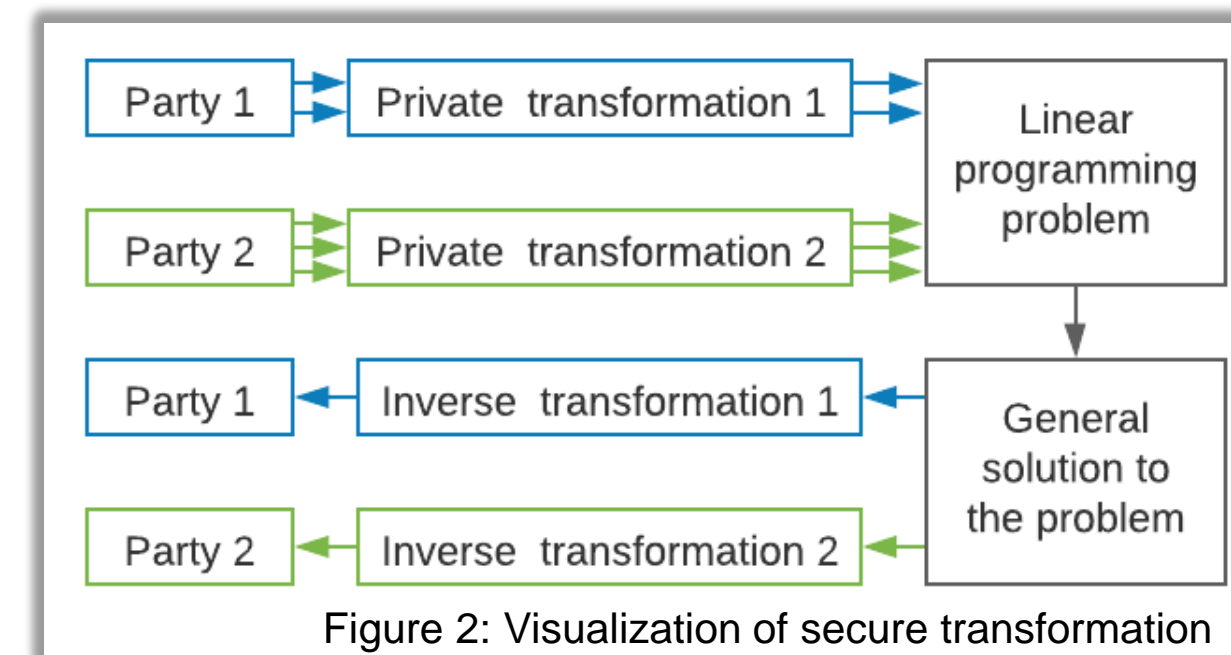


Figure 2: Visualization of secure transformation

IS ST USEFUL FOR REAL-LIFE APPLICATIONS?

- Collaborative Scheduling and Routing: can be used in last mile delivery and bin packing
- Collaborative Container Maritime Logistics: can be used in several optimization problems, such as optimizing container handling time
- Collaborative Airline Management: can be used in schedule design

4. CONCLUSIONS

- Developments for specific cases of linear programming problems
- Faster than cryptographic methods, but provides less security guarantees [4]
- Possibilities for using secure transformation in supply chain applications, theoretically
- Possibilities in computation outsourcing to cloud
- Not deployed in practice yet

LIMITATIONS

- Security is mostly heuristic [2]
- Perfect secrecy impossible when not working in a finite field [4]
- More research is needed to be conducted

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