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## 1. Research Question & Aim

**Gap in PyJobShop:** PyJobShop’s solver handles flexible job-shop makespan, earliness and tardiness, but it does not natively model or enforce *hard deadlines* under uncertainty.

**Objective:** Extend the Flexible Job Scheduling Problem pipeline with dummy-task hard deadlines and STNU–RTE\* real-time control to *guarantee* that jobs finish before their deadlines despite bounded duration variability.

### Research Sub-Questions

1. **Slack bound:** Is  $\Delta^* = \max \sum_t (\bar{d}_t - \underline{d}_t)$  both necessary & sufficient?
2. **Weight tuning:** How do  $(w_e, w_t)$  shift the average earliness–tardiness Pareto front?
3. **Noise limit:** Up to what  $\alpha$  can one policy keep  $P_{tardy} < 0.32$ ?
4. **Runtime growth:** How does end-to-end wall-time scale with  $|T|$ ?

## 2. Methodology in Four Steps

### 1. Offline CP design

- Flexible Job-Shop model with alternative machines.
- Add one *dummy deadline task* per job.
- Search a single slack  $\Delta^*$  that makes the CP model feasible.
- Grid–sweep soft weights  $(w_e, w_t)$  for the earliness-tardiness Pareto.

### 2. STNU build

- Map every task to *start* / *finish* nodes; add resource-chain edges.
- Encode duration noise  $d_t \sim \mathcal{U}[(1 - \alpha)\underline{d}_t, (1 + \alpha)\bar{d}_t]$ , with  $\alpha \in \{0.1, 0.2, 0.5, 0.8, 1.0, 2.0, 3.0\}$ .

### 3. Guarantee phase

- Check *dynamic controllability* (Java CSTNU tool).
- If DC holds, hand schedule to the real-time dispatcher RTE\*.
- Run 500 Monte Carlo simulations for the STNU considering  $d_t$ .

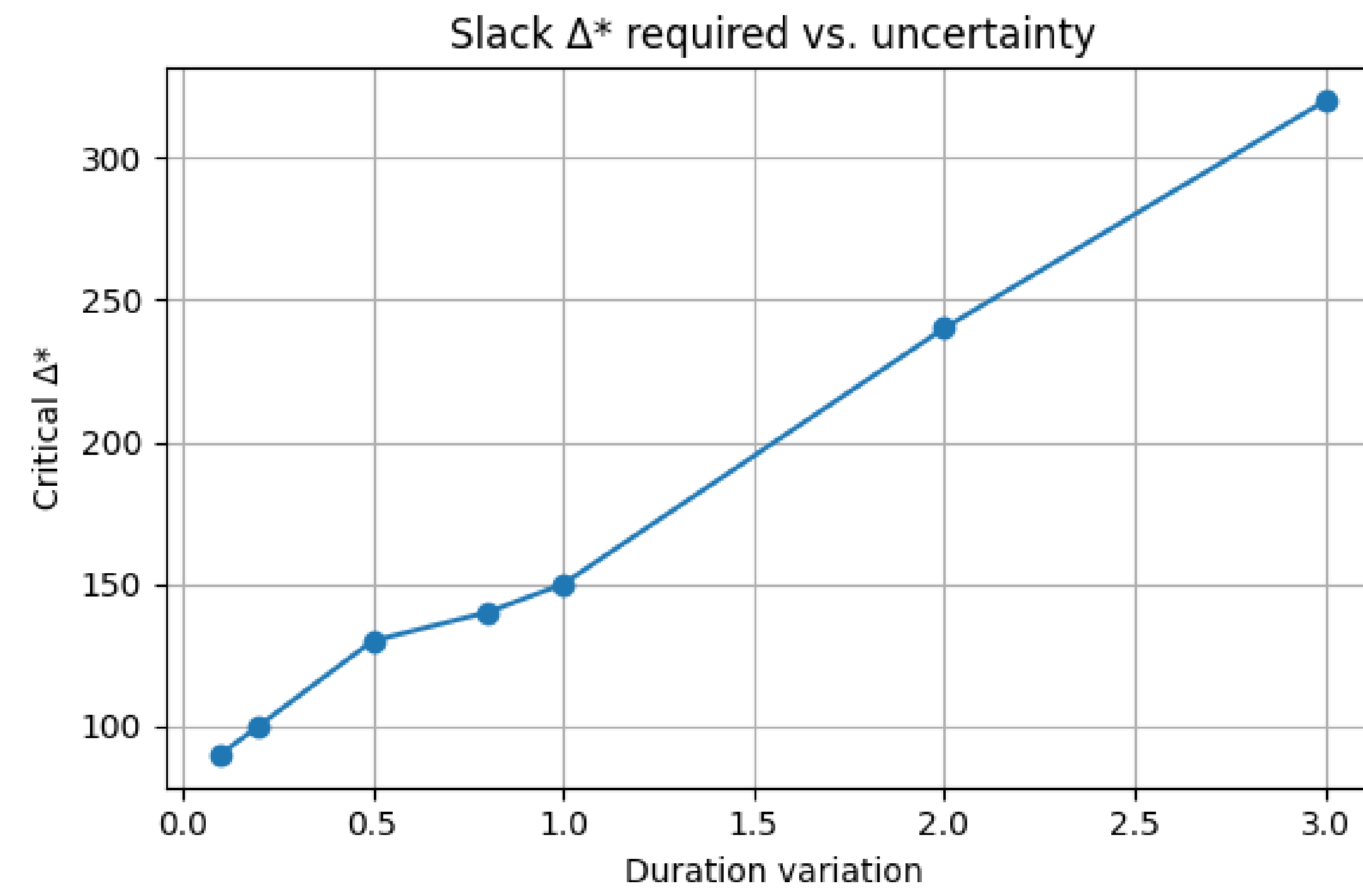
### 4. Evaluation

- *Quality metrics:*  $C_{\max}$ , mean earliness  $E$ , tardy prob.  $P_{tardy}$ .
- *Runtime metrics:* CP solve time, DC check time, RTE\* latency.
- *Benchmarks:* public Kacem 1–4 suite (4–10 jobs, 12–55 ops, 5–10 machines).

#### Key References

- [1] K. van den Houten *et al.*, “Proactive and Reactive Constraint Programming for the Flexible JSSP,” *IEEE T-SMC C* **32**, 2002.  
[2] P.H. Morris, N. Muscettola, T. Vidal, “Dynamic Controllability of STNUs,” *IJCAI* **2001**.  
[3] I. Kacem, S. Hammadi, P. Borne, “Multi-objective Optimisation for the Flexible JSSP,” *IEEE T-SMC C* **32**, 2002.  
[4] L. Hunsberger, R. Posenato, “The RTE\* Dispatcher for STNUs,” *ICAPS* **2024**.  
[5] R. Reijnen *et al.*, “Job-Shop Benchmark Environments and Instances,” arXiv 2308.12794, 2025.

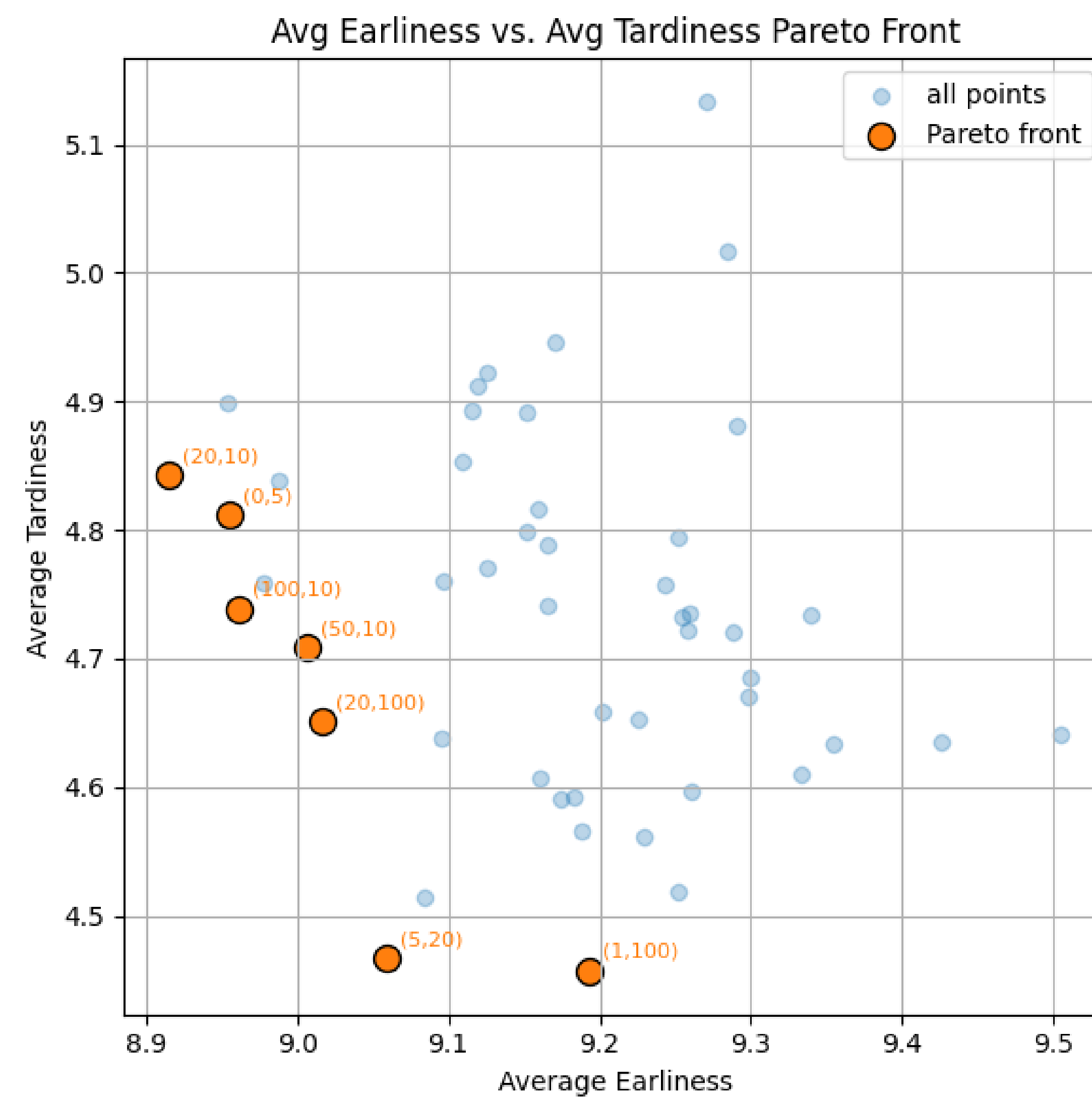
## 4. Hard-Deadline Slack Calibration (RQ1)



Duration Variations (x) vs. slack  $\Delta$  (y).

- One global slack value per duration variation  $\alpha$  guarantees *both* offline feasibility and online dynamic controllability.
- Closed-form bound  $\Delta^* = \max \sum_t (\bar{d}_t - \underline{d}_t)$  is tight to  $\pm 10$  tu on all instances.

## 5. Soft-Deadline Trade-off (RQ2)



Pareto front  $(w_e, w_t)$ . Elbow  $w_e=5/w_t=20$  achieves  $P_{tardy} < 0.32$  for  $< 2\%$  makespan hit at  $\alpha = 0.6$ .

- **Early bonus:**  $w_e=1$  cuts  $P_{tardy}$  by 10 % and trims  $C_{\max}$  1 tu.
- **Sweet spot:**  $w_e=5$  drops another 9 pp for +1 tu; gains flatten beyond.

## 6. Robustness vs Uncertainty (RQ3)

- Mean makespan rises 15 % from  $\alpha = 0$  to 1.0 (linear degradation).
- Residual earliness drops below 50 % at  $\alpha=1$ ;  $P_{tardy}$  then climbs steeply (exceeds the RQ3 target of  $P_{tardy} < 0.32$ ).
- *Heuristic trigger:* when shop-floor earliness  $< 0.5$  of nominal slack, re-optimize with larger  $\Delta$ .

## 7. Pipeline Scalability (RQ4)

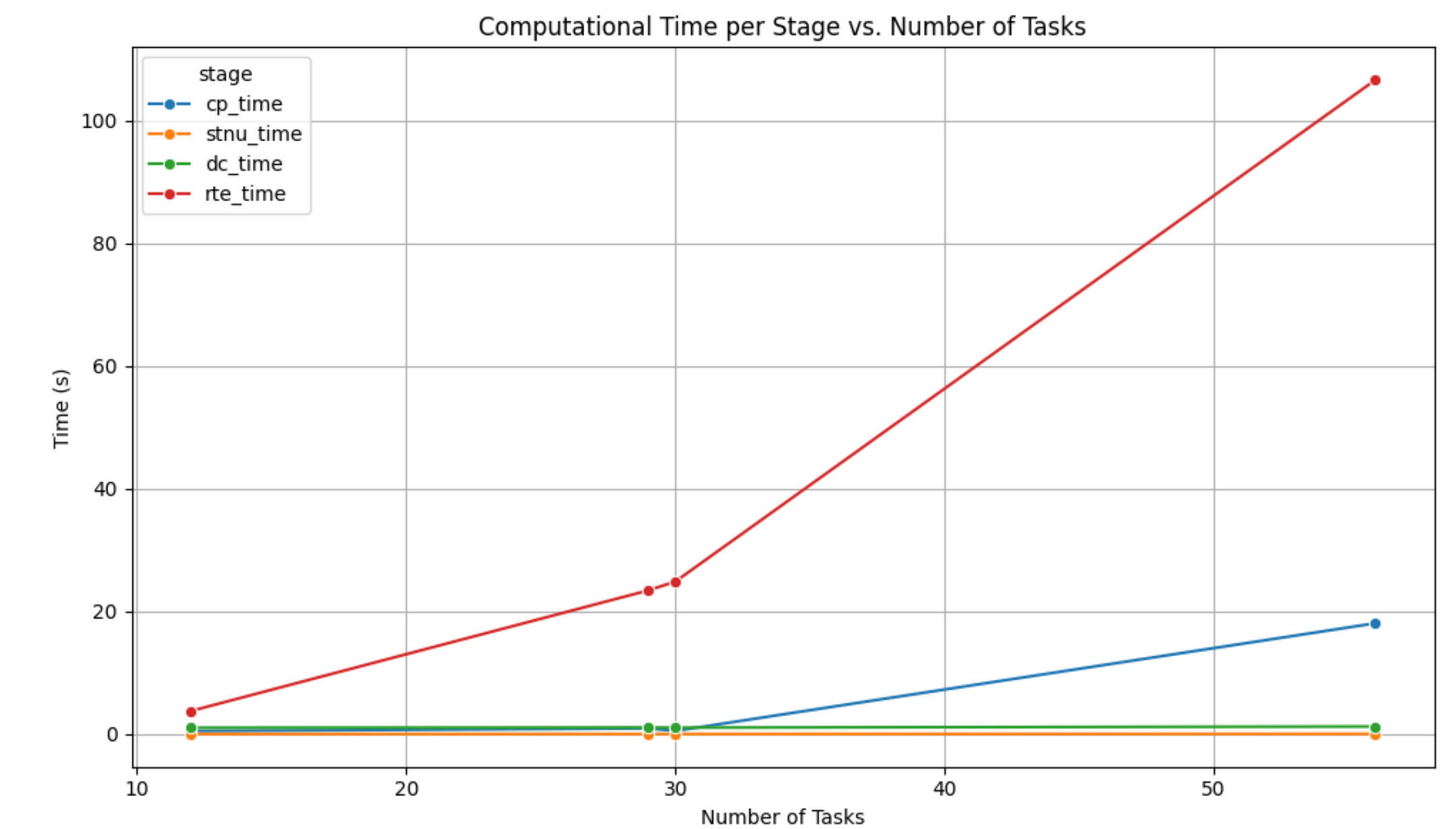


Fig. 3 — Near-linear wall-time vs. task count; DC check  $< 1\%$  of total.

- CP:  $\approx 0.33 s \times |T|$ ; 500-run RTE\*:  $\approx 1.9 s \times |T|$ .
- 55-task Kacem-4 solved & simulated in 126 s on an M1-Pro laptop.

## 8. Limitations & Future Work

- **Uncertainty model** — Uniform i.i.d. bounds ignore correlation and heavy tails; log-normal draws already break DC on Kacem-4; move toward Gamma / log-normal fits and probabilistic STNUs.
- **Slack granularity** — Same  $\Delta^*$  for every job is safe but wasteful; per-job slack budgeting plus a “distance-to-DC” surrogate could trim margins 15–20 %.
- **Auto-tuning** — Current  $(w_e, w_t)$  grid search is brute-force; Bayesian or RL tuning could track drift on the shop floor in real time.
- **Industrial validation** — Replay the pipeline on real industrial data
- **Reactive benchmark** — Compare against rolling-horizon CP and rule-based dispatch on the same  $\alpha$ -grid.

## 9. Conclusions and Recipe for Practitioners

- **Soft deadlines:** pick  $w_e \in [5, 20]$ ,  $w_t \in [0, 20]$   $P_{tardy} < 0.32$  and  $< 5\%$  makespan loss on Kacem-3/4-size shops.
- **Hard deadlines:** set  $D_j = \sum_t \min d_{jt} + \Delta^*$  with  $\Delta^* = \max \sum (\bar{d} - \underline{d})$ ; guarantees DC.
- **Health trigger:** when on-line earliness falls below 50 % of nominal slack, rerun the CP+STNU loop with a larger  $\Delta$  (empirically catches the  $\alpha > 1$  failure mode).