

1 Background

Constraint Programming: Paradigm to solve NP-Hard problems with **constraints** and **variables**.

Lazy Clause Generation: Solvers that use **explanations** for better backtracking.

Disjunctive constraint: Forces tasks not to overlap.

Propagators: Functions that prune domains variables, and return an **explanation**.

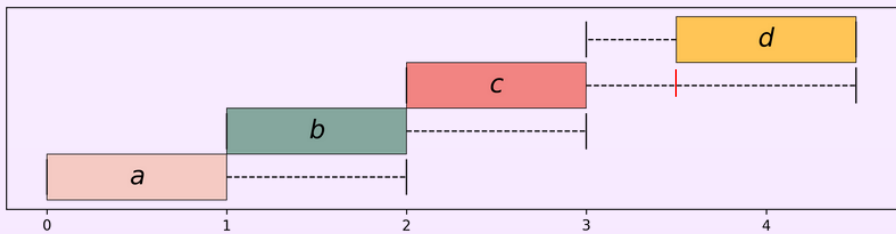
Not-First/Not-Last propagators: Shorten the range of the tasks based on whether they can not be **first** or **last** compared to a **subset** of all tasks.

Naive explanations: Input the current state of all tasks.

Vilim's explanations [1]: Input only tasks that affect propagation, with an **extended range** which will still cause a conflict.

How to propagate with **Not-Last [2]:**

1. Generate **set** of tasks that could propagate a task
2. Check if the **earliest completion time** of the set is after the **latest start time** of the task
3. Change **latest completion time** of the task
4. Generate **explanation** using set of tasks



2 Research Questions

1. Can we create **more general** explanations by iterating through all subsets of tasks?
2. What are the effects of allowing the iteration method to a max size of k sized sets?

3 Experiments

Attempt to find a better subset only when tasks is at most length k .

Tested implementations:

- Naive explanations
- Vilim's explanations
- Values of k from 2 to 5 with Vilim's explanations

Data collected:

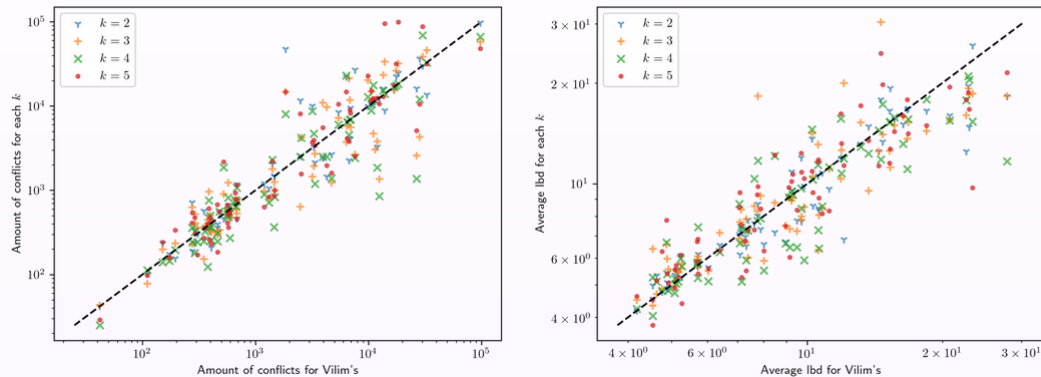
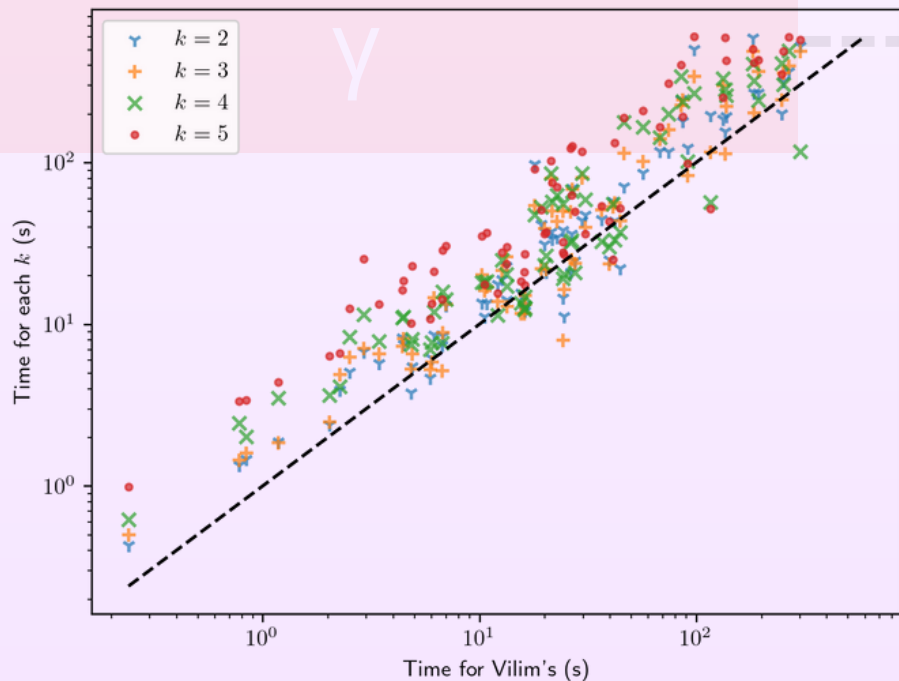
1. **Time** taken
2. Amount of **conflicts**
3. Average **LBD** [3]

Tested against 70 instances:

- LA01–LA40
- ORB01–ORB10
- 20 Generated TA instances

4 Results

- Almost all test instances are **slower** than Vilim's explanations.
- 50% **less conflicts** and lower average **LBD**.
- $k = 4$ had the best results compared to other values.
- All test instances were faster than **naive** explanations.



5 Discussion & Conclusion

Implementation of finding optimal subset had **performance issues**:

- Runtime was significantly affected by logging how often subsets were used.
- Implementation could be made better to use less memory, thus increasing speed.

Less conflicts found indicate a potential future in further exploring this field by:

- Testing **higher** values of k .
- Finding subsets faster with the use of **heuristics**.

We conclude:

- Looking through subsets of tasks does show an improvement in amount of conflicts and average LBD.
- Even with the increased complexity it still performed better than naive explanations.

References

- [1] Computing Explanations for the Unary Resource Constraint. In Lecture Notes in Computer Science, pages 396–409. Springer Berlin Heidelberg, Berlin, Heidelberg, 2005.
- [2] Petr Vilím. Global constraints in scheduling. 2007. Publisher: Univerzita Karlova, Matematicko-fyzikální fakulta.
- [3] Laurent Simon and Gilles Audemard. Predicting Learnt Clauses Quality in Modern SAT Solver. In Twenty-first International Joint Conference on Artificial Intelligence (IJCAI'09), Pasadena, United States, July 2009