

1 Introduction

- Precise localization is a challenging subtask of multi-robot navigation [1]
- Popular methods use multi-anchor setups (Fig. 1)
 - High setup cost [2]
- Single-anchor methods have been explored
 - Use (special) antenna arrays, which leads to complexity, increased power use and higher costs [3]
- **How can we develop a single-anchor localization method that does not require antenna arrays or special antennas?**

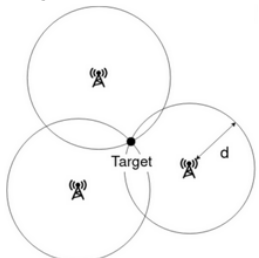


Fig. 1: Multi-anchor localization setup

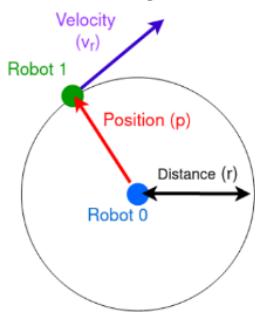


Fig. 2: Model of problem setup

2 Problem Statement

- Given are two robots $\{R_0, R_1\}$
- R_0 acts as (mobile) anchor and R_1 as target
- Measurements:
 - Distance r between robots
 - Velocity v_r of R_1 relative to R_0
- Goal: find position p

References

[1] Han Wu, Shizhen Qu, Dongdong Xu, and Chunlin Chen. Precise localization and formation control of swarm robots via wireless sensor networks. *Mathematical Problems in Engineering*, 2014:1–12, 2014.
 [2] Dimitrios Lymberopoulos and Jie Liu. The microsoft indoor localization competition: Experiences and lessons learned. *IEEE Signal Processing Magazine*, 34(5):125–140, 2017.
 [3] S. A. Zekavat. *Handbook of position location – theory, practice, and advances*, second edition. IEEE Series on Digital & Mobile Communication, Wiley-Blackwell, Hoboken, NJ, 2 edition, April 2019.
 [4] Veerachai Malayavej and Prakash Udomthanatheera. Rssi/mu sensor fusion-based localization using unscented kalman filter. In *The 20th Asia-Pacific Conference on Communication (APCC2014)*, pages 227–232, 2014.
 [5] Md. Osman Gani, Casey O'Brien, Sheikh I. Ahamed, and Roger O. Smith. Rssi based indoor localization for smartphone using fixed and mobile wireless node. In *2013 IEEE 37th Annual Computer Software and Applications Conference*, pages 110–117, 2013.

3 Motion-based Single-Anchor Localization Algorithm

- θ is the angle between v_r and p :

$$\theta(t) = \arccos \frac{\dot{r}(t)}{\|v_r(t)\|}$$

- With θ , we can get two possibilities for position p (Fig. 3):

$$p(t) = \begin{bmatrix} r(t) \cos(\alpha(t) \pm \theta(t)) \\ r(t) \sin(\alpha(t) \pm \theta(t)) \end{bmatrix}$$

where α is the angle of v_r

- We can choose one of the two possible positions when there is a change in velocity direction (Fig. 4)

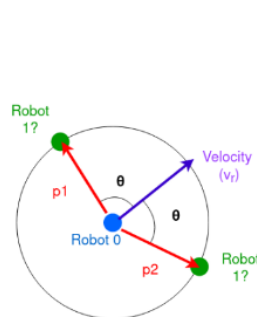


Fig. 3: Two position estimates using θ and v_r

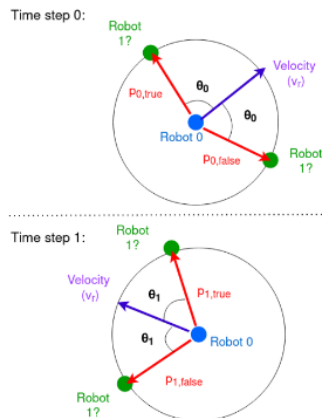


Fig. 4: When a change of velocity direction happens, we can pick one of the two position estimates

4 Noise and Filtering

- In reality, there will be noise in the measurements
- Kalman Filter
 - state estimator of the movement of the target robot
- Savitzky-Golay filter
 - To obtain filtered r and \dot{r}

5 Performance Evaluation

- Static anchor
- Target robot moving at 1 m/s, measurements every 0.5 seconds ($T = 0.5$)
 - starts at $(-9, -5)$, runs in a straight line, turns onto circular track and does 5 laps (Figure 5)

Experiment 1 - Impact of filtering techniques

- Zero-mean Gaussian noise added to the measurements ($\sigma_r = 1.0, \sigma_v = 0.1$)

- Figures 5 to 8 show the influence of noise and filtering techniques on the algorithm performance

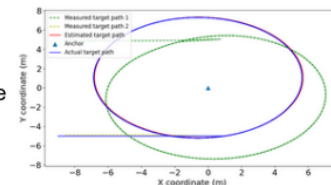


Fig. 5: Noiseless run of the simulation.

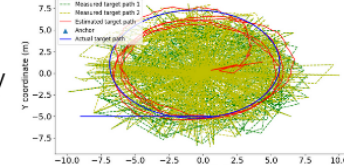


Fig. 7: Simulation with Gaussian noise added to measurements, using Kalman filter ($\sigma_r = 1.0, \sigma_v = 0.1$).

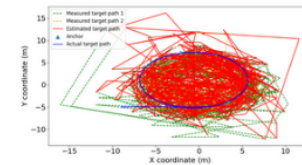


Fig. 6: Simulation with Gaussian noise added to measurements ($\sigma_r = 1.0, \sigma_v = 0.1$).

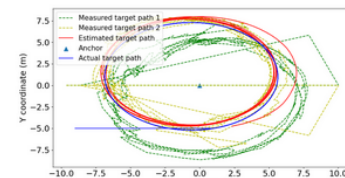


Fig. 8: Simulation with Gaussian noise added to the measurements, combining Kalman filter and Savitzky-Golay filter to filter the distance measurements ($\sigma_r = 1.0, \sigma_v = 0.1$).

- Kalman and Savitzky-Golay filters are important for accurate results
- Filtering \dot{r} dramatically improves accuracy of measured paths

Experiment 2 - RSSI-based distance measurements

- Simulation using RSSI to measure distance
- Lognormal shadowing path loss model
- RMSE of position estimate is 1.38 meters, which is comparable to other RSSI-based localization methods [4] [5]

6 Conclusions and Future work

- Developed a motion-based single-anchor algorithm that uses change in distance and velocity of target, without requiring antenna arrays
- Kalman filter and Savitzky-Golay filter were used to improve accuracy despite noisy measurements
- Precise \dot{r} is essential for accurate estimates from the proposed algorithm
- The proposed algorithm could be promising for RSSI-based localization

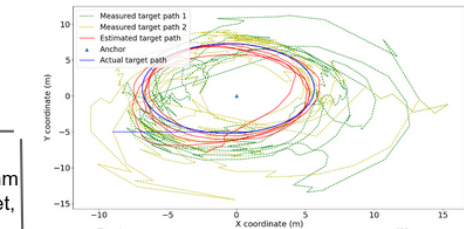


Fig. 9: Simulation using RSSI for distance measurements, according to the lognormal shadowing path loss model described in section V-A

In the future:

- Try out different robot paths
- Improve filtering of r and \dot{r}
- Expand to more robots