

Performance of Covariance Neural Networks on Rating Prediction

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1. Background

Covariance Matrix: a square matrix summarizing the second-order relationships of different variables

$Cov(u_1, u_1)$	$Cov(u_1, u_2)$	$Cov(u_1, u_3)$	$Cov(u_1, u_4)$
$Cov(u_2, u_1)$	$Cov(u_2, u_2)$	$Cov(u_2, u_3)$	$Cov(u_2, u_4)$
$Cov(u_3, u_1)$	$Cov(u_3, u_2)$	$Cov(u_3, u_3)$	$Cov(u_3, u_4)$
$Cov(u_4, u_1)$	$Cov(u_4, u_2)$	$Cov(u_4, u_3)$	$Cov(u_4, u_4)$

Covariance measures **dependence between two variables**, showing how one variable changes with another.



We can use this to **model underlying relationships** between users and items for collaborative filtering



2. Research Questions

- How do VNNs perform on rating prediction tasks using the covariance matrix as the GSO?
- How are VNNs affected by perturbations in their graph structure?

Hypothesis: VNNs will perform better than first-order models thanks to the high sparsity of the dataset.



3. Methodology

Dataset

MovieLens 100k
movielens

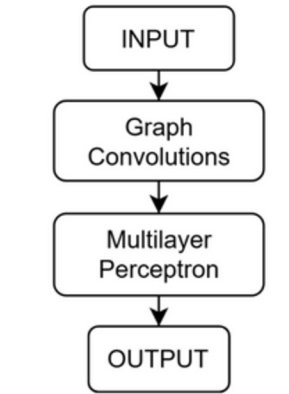
Evaluation Metric

$$RMSE = \sqrt{\frac{\sum_{i=1}^N (x_i - \hat{x}_i)^2}{N}}$$

Truth Prediction
Number of Samples

Pipeline

- Compute the **covariance matrix** from training data. Use this for the model's **Graph Shift Operator (GSO)**
- Mask values** from the interaction matrix. Use these masked values for evaluation, and the remainder for forward passes.
- Train** the model.
- Evaluate** on the **test set**.



The VNN Architecture

Experiments

Robustness

Force the model to use only a sample of the training data to create the GSO, then train the model and evaluate its performance

Stability

Introduce perturbations into the GSO of a trained model and evaluate its performance



5. Conclusions and Limitations

Conclusion

- VNNs are capable of performing strongly in rating prediction tasks by leveraging second-order relationships using the covariance matrix.
- The stability of VNNs depend on the density of the network and may be prone to oversmoothing.

Limitations

- Transductive Pipeline
- Dataset may be too sparse, so covariance estimate may be too noisy

Future Work

- Combine Architectures
- Better Imputation
- Regularization to overcome oversmoothing



4. Results

Final Model Performance:
0.9682, std. dev of 0.00553

Comparison to Baselines

Model	RMSE
VNN	0.9682
Global Mean	1.1537
Random	1.8762
Identity GSO	1.0695
All-ones GSO	0.9823

The VNN is able to beat the baseline models, demonstrating that it is **properly learning**.

Comparison to Other Models

Model	RMSE
VNN	0.9682
MC	0.973
IMC	1.653
GMC	0.996
GRALS	0.945
sRGCNN	0.929
GC-MC	0.905

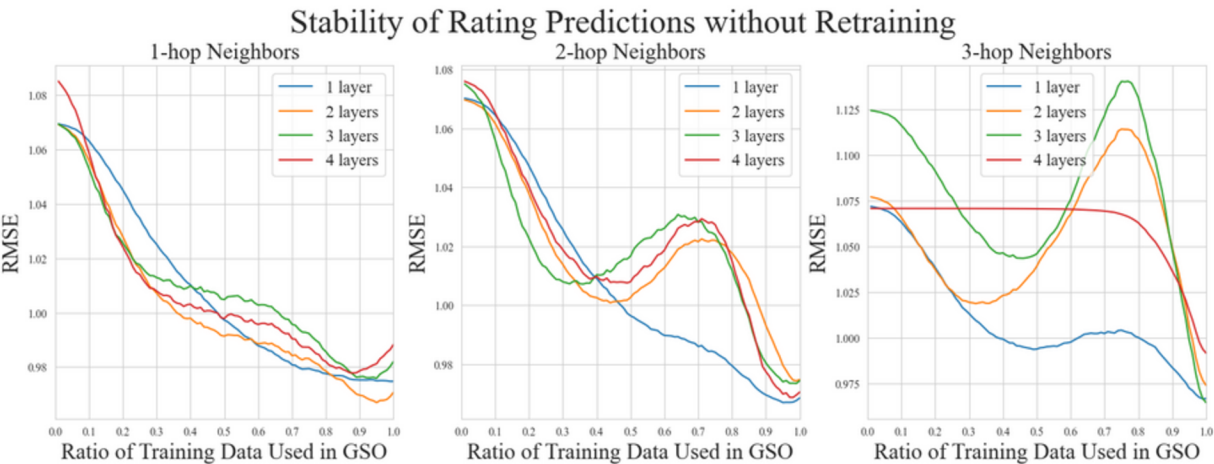
While able to **beat simpler matrix completion models**, the VNN **struggles to beat more advanced models** that are able to grasp more relationships.

Robustness Experiment Results



The VNN's performance degrades as the covariance matrix is perturbed, implying the model **learns second-order relationships**.

Stability Experiment Results



The model's performance **decreases gradually for the 1-hop VNN**, no matter how many layers. These display **relatively stable performance when compared to the 2-hop and 3-hop VNNs**. This is most likely due to **oversmoothing**. As the network gets deeper, the effects become more exaggerated.

